Terrestrial Parallax in the Low-mass Event MOA-2011-BLG-274 and A Preliminary Search for Low-mass Objects in the Database of the WISE Space Mission

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MOA-2011-BLG-274

- $t_E = 3.06$ days
- Either fast moving or small mass lens
- $\rho = 0.0112$, in typical events $\rho = 0.001$
- $\rho = \theta_S/\theta_E$
- Either source star is 10x as large or mass (Einstein radius) is 10x as small
- Source star has usual luminosity. Thus, very low mass lens
Differences in analysis

• This event has also been analysed in the paper:
  ‘Characterizing lenses and lensed stars of high magnification gravitational microlensing events with lenses passing over source stars’, JY Choi et al, arXiv:1111.4032

Differences:
• Perth data rereduced because it appeared relatively noisy compared to Auckland data with similar sized telescopes, and Perth weather was excellent.
• Renormalised error bars for all datasets
• In particular, MOA data renormalised at baseline and at peak magnification
• Included OGLE data
Parallax measurements

- Calculation of $\chi^2$ for each pair of parallax values
- Shows a best fit at
  - $\pi_{EE} = -2$
  - $\pi_{EN} = 10$
- Large area of uncertainty
Parallax interpolated

- Interpolation of previous graph.
- Lines at 2 sigma and 3 sigma
Testing change of $\theta$

- Just done to test our program
- With no planets, changing the source star track angle should have no effect
- Rectangular pixels are used for the magnification map, could cause small deviations
- The parallax plot with a changed value of theta = 0.3 shows only a very small difference, $<1 \chi^2$
Marginalisation of t0

- For each fixed value of t0 a minimum is found
- Gives error estimates – an increase of 1 $\chi^2$ is one sigma.
- 0.00001 interval between points (~1 sec)
- 1 sigma = ~2.5 divisions =
  - = 0.000025 days
  - = ~2 seconds
- So we can measure time differences with fairly good accuracy.
Source star parameters

- \((V-I)_0 = 0.76 \text{ and } I_0 = 17.96\) (private communication from A. Gould using CTIO field stars)

- Assuming the source distance is in the bulge at 8 kpc, the above implies \(M_I = 3.445\) and \(M_V = 4.205\)

- The nearest star on isochrones of L. Girardi et al (A&A 391, 195, 2002) with age = 10 billion years and solar abundance \(Z = 0.019\) has temp = 5688K, surface gravity \(\log g = 4.083\) and radius \(r_s/r_{\text{solar}} = 1.492\). Hence angular source star radius \(\theta_s = 0.87\) \(\mu\text{as}\) (0.85 \(\mu\text{as}\) obtained by A. Gould).


<table>
<thead>
<tr>
<th></th>
<th>V</th>
<th>R</th>
<th>I</th>
</tr>
</thead>
<tbody>
<tr>
<td>u</td>
<td>0.619</td>
<td>0.564</td>
<td>0.469</td>
</tr>
</tbody>
</table>
## Limb darkening coefficients

<table>
<thead>
<tr>
<th></th>
<th>Filter Colour</th>
<th>Passband</th>
<th>( u )</th>
<th>( u ) (A.Gould)</th>
<th>( u ) compromise</th>
</tr>
</thead>
<tbody>
<tr>
<td>OGLE</td>
<td>I</td>
<td>I</td>
<td>0.47</td>
<td>0.45</td>
<td>0.47</td>
</tr>
<tr>
<td>MOA</td>
<td>Red</td>
<td>((R+I)/2)</td>
<td>0.51</td>
<td>0.49</td>
<td>0.51</td>
</tr>
<tr>
<td>Kumeu, Auckland</td>
<td>Red</td>
<td>((2R+I)/3)</td>
<td>0.52</td>
<td>0.52</td>
<td>0.52</td>
</tr>
<tr>
<td>Perth, Farm Cove</td>
<td>White (no filter)</td>
<td>((V+R)/2)</td>
<td>0.58</td>
<td>0.51</td>
<td>0.53</td>
</tr>
</tbody>
</table>

\( u = \) linear limb darkening coefficient  
\( (V+R)/2 = \) unfiltered + reddening from dust
Calculation of lens mass/distance

- \( \pi_E = 10.20 \)
- \( r_s = 1.492 \times r_{\text{solar}} = 1.492 \times 6.96 \times 10^8 \text{ m} = 1.04 \times 10^9 \text{ m} \)
- \( \rho = 0.0112 \)

- \( r'_E = \text{AU}/\pi_E = 1.5 \times 10^{11} \text{ m}/10.20 = 1.47 \times 10^{10} \text{ m} \)
- \( r''_E = r_s/\rho = 1.04 \times 10^9 \text{ m} /0.0112 = 9.27 \times 10^{10} \text{ m} \)
- \( D_s = 8 \text{ kpc} = 2.42 \times 10^{20} \text{ m} \)
Calculation of lens mass/distance

- \(1/r_E = 1/r_E' + 1/r_E''\) (from the geometry of the previous diagram)
- \(r_E = 1.27 \times 10^{10} \text{ m} = 0.085 \text{ AU}\)
- \(D_L = D_S r_E/r_E'' = 1.09 \text{ kpc}\)
- \(r_E = \sqrt{(4GM_L/c^2)} \times \sqrt{(D_L D_{LS}/D_S)}\)
- \(M_L = r_E^2 c^2 D_S/4G D_L D_{LS} = 1.86 \times 10^{27} \text{ kg} = 0.97 \text{ MJ}\)
Result – Jupiter mass object

- The 2 sigma error contour gives range of 0.5 to 2 Jupiter masses
- This is a fairly large range, but not too bad for microlensing. Uncertainties in mass are usual.
Peak magnification times

<table>
<thead>
<tr>
<th>Telescope</th>
<th>Tmax (HJD)</th>
<th>Tmax – Tmax,moa (seconds)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Perth</td>
<td>5742.005536</td>
<td>19</td>
</tr>
<tr>
<td>Farm Cove</td>
<td>5742.005472</td>
<td>12</td>
</tr>
<tr>
<td>Kumeu</td>
<td>5742.005470</td>
<td>12</td>
</tr>
<tr>
<td>MOA</td>
<td>5742.005316</td>
<td>-</td>
</tr>
</tbody>
</table>

These time differences show that parallax is detectable in this event.
Calculation of trajectory

• Best fit \( u_{\text{min}} = 0.00255 \)
• Hence \( u_{\text{min, observer plane}} = 0.00255 \times r_E \)
  \[ = 0.00255 \times 1.47 \times 10^{10} \text{ m} \]
  \[ = 37,485 \text{ km} = 5.88 \, r_{\text{Earth}} \]
• Direction = \( \tan^{-1}(-2/10) = 11.3^\circ \) west of North
• Speed = \( r_E'/t_E \)
• \( \approx 1.47 \times 10^{10} \text{ m} / \text{3 days} \approx 60 \text{ km/sec} \)
• Hence \( t_{0, \text{Auckland}} - t_{0, \text{Mt John}} \approx 650 \text{ km} / 60 \text{ km s}^{-1} \approx 11 \text{ seconds} \) (observed \( \approx 12 \text{ secs} \))
• Note that the peak magnification at FCO was higher than that at Perth which had the same limb darkening. Hence trajectory is east of Australasia as shown below, not west.
Track in observer plane

5.9 earth radii away.
Detectability of exomoons

- This object has a mass similar to that of Jupiter.
- Could have orbiting moons (although no sign yet in light curve)
## Jupiter’s Moons

<table>
<thead>
<tr>
<th></th>
<th>Mass (kg)</th>
<th>Mass ratio $q = M/M_J$</th>
<th>Orbital radius (m)</th>
<th>Orbital radius $r_E$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Io</td>
<td>$8.93 \times 10^{22}$</td>
<td>$4.7 \times 10^{-5}$</td>
<td>$4.22 \times 10^8$</td>
<td>0.033</td>
</tr>
<tr>
<td>Europa</td>
<td>$4.80 \times 10^{22}$</td>
<td>$2.5 \times 10^{-5}$</td>
<td>$6.71 \times 10^8$</td>
<td>0.052</td>
</tr>
<tr>
<td>Ganymede</td>
<td>$1.48 \times 10^{23}$</td>
<td>$7.8 \times 10^{-5}$</td>
<td>$1.07 \times 10^9$</td>
<td>0.083</td>
</tr>
<tr>
<td>Callisto</td>
<td>$1.08 \times 10^{23}$</td>
<td>$5.7 \times 10^{-5}$</td>
<td>$1.88 \times 10^9$</td>
<td>0.146</td>
</tr>
</tbody>
</table>

- Mass ratios and orbital radii are both an order of magnitude too small to be detected by gravitational lensing.
- Cold look for larger moons further out
Possibility of adding a moon

$\chi^2$ for each pair of parameters, distance and mass

Star diameter = 1000 pixels
Our code is good for free floating planets – a larger star reduces the effect of the rectangular pixels
Possibility of adding a moon

- Same plot again in 3D
- Could be small moons in close orbit.
- Larger moons close to the Einstein radius are excluded
Light curve with moon

Model with a moon orbiting
Mass ratio 0.0005
Distance 0.9 \( r_E \)
– increases \( \chi^2 \) by 300
Can see a deviation in the residuals
Larger moon

With a moon twice as large, there is a very noticeable deviation.
Mass ratio 0.001
Distance 0.9 $r_E$

A moon this size can be excluded
A smaller moon produces a smaller deviation (but still a noticeable increase in $\chi^2$).
Mass ratio 0.0002
Distance 0.9 $r_E$

More searching may find such a moon
Still to do

• Search for a stellar companion to this planet.
• Because the light curve is so good we should be able to exclude a star out to a large distance.
WISE data analysis, by John Bray

- Puzzle – surprisingly high number of free-floating Jupiters!
- Sumi et al found 1.8 free-floating Jupiters per star (Nature 473, 349, 2011)
- Cassan et al report 17% of stars host an orbiting Jupiter (Nature 481, 167, 2012)
- The measurements suggest either most Jupiters are ejected, or most free-floating Jupiters are born free (i.e. they are very cool sub-brown-dwarfs).
- May be able to test the second possibility by searching for very cool sub-brown-dwarfs (late Y dwarfs) in the WISE database.
- We merely wish to bring the WISE mission to the attention of the microlensing community, we are not attempting to compete with the WISE group.
WISE telescope

40cm widefield telescope cooled by solid hydrogen cryostat to <12K, detectors to <7.5K
WISEPassbands

(E. Wright et al arXiv:1008.0031)
WISE Orbit

WISE coverage is very redundant at the poles

1 frame 1 orbit 2 orbits Many orbits

(E. Wright et al arXiv:1008.0031)
WISE Coverage

2784184 frames thru end of mission

WISE has surveyed the whole sky twice.
WISE colour-colour populations

- Emission by cool brown dwarfs at 4.6\textmu m due to lack of methane absorption
Search region (preliminary data only)
Thanks to

- Michael Albrow
- Christine Botzler
- John Bray
- Sean Davidson
- Dimitri Douchin
- Andy Gould
- Yvette Perrott
- Lydia Philpott
Best fit

• From first parallax run
• $U_{\text{min}}$ 0.00255
• $\theta$ 0.5
• $S_{\text{sr}}$ 0.0112
• $t_0$ 5742.00565
• $t_E$ 3.06
• $\pi_{\text{EE}}$ -2
• $\pi_{\text{EN}}$ 10
• $\chi^2$ 1350.83349
Parameters for two moons

- Mass 0.00051
  - $0.00359 \ 0.5 \ 0.0112 \ 5742.00526 \ 3.07 \ -2 \ 10$
  - $\chi^2 = 1661.9592$

- Mass 0.00101
  - $0.00423 \ 0.5 \ 0.0112 \ 5472.00508 \ 3.04 \ -2 \ 10$
  - $\chi^2 = 2389.0983$

- Umin changed a lot due to the exomoon